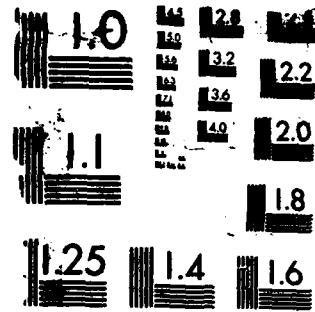


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REPORT DOCUMENTATION PAGE				Form Approved OMB No 0704-0188 Exp Date Jun 30, 1986						
1a REPORT SECURITY CLASSIFICATION Unclassified		1b RESTRICTIVE MARKINGS								
2a SECURITY CLASSIFICATION AUTHORITY		3 DISTRIBUTION/AVAILABILITY OF REPORT Approved for public release; distribution unlimited								
2b DECLASSIFICATION/DOWNGRADING SCHEDULE										
4 PERFORMING ORGANIZATION REPORT NUMBER(S)		5 MONITORING ORGANIZATION REPORT NUMBER(S)								
6a NAME OF PERFORMING ORGANIZATION Ballistic Research Laboratory	6b OFFICE SYMBOL (If applicable) SLCBR-TB-S	7a NAME OF MONITORING ORGANIZATION								
6c ADDRESS (City, State, and ZIP Code) Aberdeen Proving Ground, MD 21005-5066		7b ADDRESS (City, State, and ZIP Code)								
8a NAME OF FUNDING/SPONSORING ORGANIZATION	8b OFFICE SYMBOL (If applicable)	9 PROCUREMENT INSTRUMENT IDENTIFICATION NUMBER								
8c ADDRESS (City, State, and ZIP Code)		10 SOURCE OF FUNDING NUMBERS <table border="1"><tr><td>PROGRAM ELEMENT NO</td><td>PROJECT NO</td><td>TASK NO</td><td>WORK UNIT ACCESSION NO</td></tr></table>			PROGRAM ELEMENT NO	PROJECT NO	TASK NO	WORK UNIT ACCESSION NO		
PROGRAM ELEMENT NO	PROJECT NO	TASK NO	WORK UNIT ACCESSION NO							
11 TITLE (Include Security Classification) Numerical Integration of a System of Equations in Thermoviscoplasticity										
12 PERSONAL AUTHOR(S) Batra, Romesh C., University of Missouri-Rolla; Wright, Thomas W., Ballistic Research Lab.										
13a TYPE OF REPORT Memorandum	13b TIME COVERED FROM <u>7/85</u> TO <u>7/86</u>	14 DATE OF REPORT (Year, Month, Day)		15 PAGE COUNT						
16 SUPPLEMENTARY NOTATION										
17 COSATI CODES <table border="1"><tr><th>FIELD</th><th>GROUP</th><th>SUB-GROUP</th></tr><tr><td>20</td><td>11</td><td></td></tr></table>	FIELD	GROUP	SUB-GROUP	20	11		18 SUBJECT TERMS (Continue on reverse if necessary and identify by block number) Shear bands, finite element method, Crank-Nicolson method			
FIELD	GROUP	SUB-GROUP								
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19 ABSTRACT (Continue on reverse if necessary and identify by block number) A set of nonlinear and coupled equations governing the thermomechanical deformations of a viscoplastic body undergoing simple shearing deformations is integrated in time by using the Forward-Difference-Galerkin-Finite-Element (FDGFE) method and the Crank-Nicolson-Galerkin-Finite-Element (CNGFE) method. In the latter scheme the number of unknown functions is increased so that the governing equations involve only first order spatial derivatives. It is shown that the solutions obtained by the two methods agree qualitatively but the CNGFE method seems to introduce considerable damping into the system. However, the time increment needed to obtain a stable solution by the CNGFE method is 200 times that required by the FDGFE method.										
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22a NAME OF RESPONSIBLE INDIVIDUAL Wright, Thomas W.		22b TELEPHONE (Include Area Code) 301-278-6046		22c OFFICE SYMBOL SLCBR-TB-S						

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I. INTRODUCTION

A thorough study of processes such as metal forming, impact, penetration and adiabatic shear banding requires integration, with respect to time, of a coupled system of nonlinear partial differential equations. For the model representing one of these phenomena to be somewhat realistic, it should incorporate such effects as strain hardening, strain-rate hardening and thermal softening. These effects are exhibited by most metals undergoing large deformations at high strain rates. For homogeneous and simple shearing deformations of such viscoplastic materials, the adiabatic shear stress-shear strain curve is generally concave towards the origin and has a peak in it. At this peak, the effect of thermal softening equals the combined effect of strain and strain-rate hardening. Under further loading, the thermal softening overtakes the strain and strain-rate hardening, and consequently the shear stress required to maintain simple shearing deformations of the body decreases with an increase in shear strain.

In essentially all practical problems enumerated above, one needs to integrate the governing equations well beyond the peak in the stress-strain curve. Whereas it is a trivial matter to carry out this integration when the deformations are homogeneous, it is a rather time consuming endeavor to do so for non-homogeneous deformations even when the deformations are one-dimensional. Herein we discuss our experience with two methods, the forward-difference scheme and the Crank-Nicolson method. In each case, the governing partial differential equations were first reduced to a set of ordinary differential equations by using the Galerkin finite element method. Also in the case of the Crank-Nicolson method the number of unknowns at each point was increased from five to eight so that only first order spatial derivatives of the unknowns appeared in the equations. We should point out that the governing equations are stiff and no artificial viscosity was introduced in either case. Of course, the Crank-Nicolson method has artificial viscosity inherently built into it.

Our numerical experiments reveal that the Crank-Nicolson-Galerkin-Finite-Element (CNGFE) method allows the use of time steps at least two orders of magnitude larger than those permitted by the Forward-Difference-Galerkin-Finite-Element (FDGFE) scheme and still gives an acceptable stable solution. It is conceivable that the efficiency of the forward-difference scheme used herein would improve if auxiliary variables were introduced, as was done for the Crank-Nicolson method, so that only first order spatial derivatives appeared in the governing equations.

We refer the reader to excellent books¹⁻⁴ and references given therein for a discussion of various numerical integration techniques. We note that Chandra and Mukherjee⁵ recently used the forward-difference method to integrate a stiff set of partial differential equations somewhat akin to ours. They used an Euler type scheme with automatic time-step control. However, selecting parameters that control the time-increment automatically is a hard task.

We add that in an earlier paper⁶ the emphasis was on reporting the complete set of solutions, obtained by using the CNGFE method, to equations studied herein. In this paper, we provide details of the two numerical

techniques and compare results, for one variable only, obtained by using the two methods.

A. Formulation of the Simple Shearing Problem

We study the simple shearing deformations of a dipolar visco-plastic material and assume that all of the variables have been non-dimensionalized. Thus the body occupies the infinite slab bounded by the planes $y = \pm 1$. Referring the reader to Reference 6 for details, we note that the governing equations are

$$\dot{v} = \frac{1}{\rho} (s - \tau \sigma_{yy})_y , \quad (1)$$

$$\dot{\theta} = k \theta_{yy} + \Lambda (s^2 + \sigma^2) , \quad (2)$$

$$\dot{s} = u(v_y - \Lambda s) , \quad (3)$$

$$\dot{\sigma} = \tau u(v_{yy} - \frac{\Lambda}{\ell} \sigma) , \quad (4)$$

$$\dot{\psi} = \Lambda (s^2 + \sigma^2) / (1 + \frac{\psi}{\psi_0})^n , \quad (5)$$

$$\Lambda = \max \left[0, \left\{ \left[\frac{(s^2 + \sigma^2)^{\frac{1}{2}}}{(1 + \frac{\psi}{\psi_0})^n (1 - a\theta)} \right]^{\frac{1}{m}} - 1 \right\} / (b(s^2 + \sigma^2)^{\frac{1}{2}}) \right] , \quad (6)$$

with boundary conditions

$$v(\pm 1, t) = \pm 1 , \quad (7)$$

$$\theta_{yy}(\pm 1, t) = 0 , \quad (8)$$

$$\sigma(\pm 1, t) = 0 , \quad (9)$$

and a suitable set of initial conditions. Equations (1) and (2) express, respectively, the balance of linear momentum and internal energy. Herein v is the velocity of a material particle, ρ its mass density, u its shear modulus, ℓ a characteristic material length, k its thermal conductivity, θ its temperature change from that in the reference configuration, and s and σ may be interpreted as the shear stress and the dipolar shear stress. A superimposed dot indicates material time differentiation and a comma followed by y signifies partial differentiation with respect to y . The constitutive relations (3) - (6) give one possible model of viscoplastic

materials. Equation (6) implies that the plastic parts, Λs and $\Lambda s/\lambda$, of the strain rate and the dipolar strain-rate vanish when

$$(s^2 + \sigma^2)^{\frac{1}{2}} \leq (1 + \frac{\psi}{\psi_0})^n (1 - a\theta).$$

Because of the non-dimensional variables being used, the initial yield stress equals one in an isothermal and quasistatic reference test. The material parameters ψ and n describe the strain hardening of the material, a the thermal softening, and b and m the strain-rate sensitivity of the material.

We presume that the initial values of θ , s and ψ are symmetric and of v and σ antisymmetric in y and seek solutions of equations (1) through (6) with the same symmetry. Thus the problem is to be studied over the spatial domain $[0, 1]$ and the boundary conditions become

$$v(1, t) = 1, \quad v(0, t) = 0, \quad (10)$$

$$\theta_{,y}(1, t) = 0, \quad \theta_{,y}(0, t) = 0, \quad (11)$$

$$\sigma(1, t) = 0, \quad \sigma(0, t) = 0. \quad (12)$$

For the initial conditions we take

$$v(y, 0) = y, \quad \sigma(y, 0) = 0, \quad \psi(y, 0) = \bar{\psi}, \\ \theta(y, 0) = \bar{\theta}_0 + \bar{\theta}(y), \quad (13)$$

$$s(y, 0) = s_0 = (1 + \frac{\psi}{\psi_0}) (1 + b\Lambda s_0)^m (1 - a\theta(y, 0)).$$

The values of $\bar{\theta}_0$, s_0 and $\bar{\psi}$ are such that, during homogeneous deformations of the block, the shear stress s_0 and the strain corresponding to $\bar{\psi}$ lie on the shear stress-shear strain curve for the material. Λ in Eq. (13)₅ is given by Eq. (5) with $\theta = \bar{\theta}_0$, $s = s_0$, $\psi = \bar{\psi}$, $\sigma = 0$. The function $\bar{\theta}$ describes the aberration in the initial temperature distribution and will result in non-homogeneous deformations of the body.

B. Numerical Integration of Governing Equations

1. Crank-Nicolson-Galerkin-Finite-Element Method.

With the auxiliary variables

$$u = v_{,y}, \quad \xi = \theta_{,y}, \quad p = \sigma_{,y}, \quad (14)$$

we can rewrite equations (1) - (4) as

$$\dot{v} = \frac{1}{\rho} (s - \ell p),_y , \quad (15)$$

$$\dot{\theta} = kg,_y + \Lambda(s^2 + \sigma^2) , \quad (16)$$

$$\dot{s} = \mu(u - \Lambda s) , \quad (17)$$

$$\dot{\sigma} = \ell\mu(u,_y - \frac{\Lambda}{\ell} \sigma) . \quad (18)$$

Thus only first order spatial derivatives of the unknowns $v, \theta, s, \sigma, u, g$ and p appear in the governing equations. Let H^1 denote the space of functions defined on $[0, 1]$ the square of whose first order derivative is integrable over $[0, 1]$. We approximate the unknown functions v, θ, s etc. by a linear combination of the finite element basis functions $\{\phi_i(y), i=2, \dots, N\}$ in an N -dimensional subspace of H^1 . For example,

$$v(y, t) = v_i(t)\phi_i(y). \quad (19)$$

Throughout this article, a repeated index implies summation over the range of the index. Using Galerkin's⁷ method we thus reduce equations (14) through (18) to the following set of equations.

$$M_{ij}u_i = -Q_{ij}v_i , \quad (20)$$

$$M_{ij}g_i = -Q_{ij}\theta_i , \quad (21)$$

$$M_{ij}p_i = -Q_{ij}\sigma_i , \quad (22)$$

$$M_{ij}\dot{v}_i = -Q_{ij}s_i + \frac{\ell}{\rho} Q_{ij}p_i , \quad (23)$$

$$M_{ij}\dot{\theta}_i = -kQ_{ij}g_i + \Lambda_i p_{ij} , \quad (24)$$

$$M_{ij}\dot{s}_i = \mu M_{ij}u_i - \mu \Lambda_i s_k R_{ijk} , \quad (25)$$

$$M_{ij}\dot{\sigma}_i = -\mu \ell Q_{ij}u_i - \mu \Lambda_i \sigma_k R_{ijk} , \quad (26)$$

where

$$M_{ij} \equiv \int_0^1 \phi_i \phi_j dy = M_{ji}, \quad (27)$$

$$Q_{ij} \equiv \int_0^1 \phi_i \phi_j, y dy, \quad (28)$$

$$\tilde{Q}_{ij} \equiv Q_{ij} - (\phi_i \phi_j) \Big|_0^1, \quad (29)$$

$$R_{ijk} \equiv \int_0^1 \phi_i \phi_j \phi_k dy = R_{ikj} = R_{kij}, \quad (30)$$

$$P_{ij} \equiv \int_0^1 \phi_i \phi_j (s^2 + \sigma^2) dy = P_{ji}. \quad (31)$$

We note that because of the nonlinear dependence of P_{ij} and Λ upon s , σ , ψ and θ , the coupled set of ordinary differential equations (20)-(26) is not that easy to integrate. The matrices M_{ij} , Q_{ij} , \tilde{Q}_{ij} , R_{ijk} and P_{ij} have been evaluated by using the linear basis functions. Also $v_i(t)$ denotes the velocity of node i at time t .

In the Crank-Nicolson method, equations (20)-(26), assumed to hold at time $(t + \Delta t/2)$, are used to predict the values of $v, \theta, s, \sigma, g, p, u$ and ψ at time $(t + \Delta t)$ from a knowledge of their values at time t . This is accomplished by approximating $\dot{\theta}_i(t + \Delta t/2)$ by $(\theta_i(t + \Delta t) - \theta_i(t))/\Delta t$, $\dot{\theta}_i(t + \Delta t/2)$ by $(\theta_i(t + \Delta t) + \theta_i(t))/2$, etc. and by first evaluating the nonlinear terms on the right hand side of (20)-(26) at time t . The resulting system of linear algebraic equations is solved for $v_i(t + \Delta t)$ etc., the right-hand side in equations (20)-(26) is now evaluated at time $(t + \Delta t/2)$ and the system of equations solved again for $v_i(t + \Delta t)$ etc. This iterative process is continued till, at each nodal point,

$$|\frac{\Delta v}{v}| + |\frac{\Delta \theta}{\theta}| + |\frac{\Delta s}{s}| + |\frac{\Delta \psi}{\psi}| + |\Delta \sigma| + |\Delta g| + |\Delta p| + |\Delta u| \leq \epsilon \quad (32)$$

where subscript i has been dropped from v_i etc., Δv denotes the difference between the newly found value of v and that used to compute the right-hand side in (20)-(26), and ϵ is a preassigned small number. The initial conditions (13) were used to find $v_i(0)$ etc.

2. Forward-Difference-Galerkin-Finite-Element Method.

In this method the field equations (1) and (2) were first cast into a weak form. Let ϕ and ψ be two smooth functions defined on $[0, 1]$ such that $\phi(0) = \phi(1) = 0$. With equations (1) and (2) multiplied through by ϕ and ξ respectively and with use of the boundary conditions (10)-(12), integration by parts over the interval $[0, 1]$ gives

$$\int_0^1 \dot{v}\phi dy = -\frac{1}{\rho} \int_0^1 s\phi_{,y} dy - \frac{\lambda}{\rho} \int_0^1 \sigma\phi_{,yy} dy , \quad (33)$$

$$\int_0^1 \dot{\theta}dy = -k \int_0^1 \theta_{,y}\xi_{,y} dy + \int_0^1 \Lambda(s^2 + \sigma^2)\xi dy , \quad (34)$$

Let the interval $[0, 1]$ be divided into $(N-1)$ subintervals, not necessarily of equal length. Thus N is the number of nodes in the mesh. Let ϕ_i^0, ϕ_i^1 ($i=1, 2, \dots, N$) be the Hermite basis functions⁷, and ϕ_i ($i=1, 2, \dots, N$) the finite element basis functions introduced previously (e.g. see Eqn. (19)). We impose the following approximations on v and θ .

$$v(y, t) = v_i(t) \phi_i^0(y) + \dot{v}_i(t) \phi_i^1(y) , \quad (35)$$

$$\theta(y, t) = \theta_i(t) \phi_i(y) . \quad (36)$$

Here $\dot{v}_i(t)$ is the value of v , at the node i at time t . Hermite basis functions ϕ_i^0, ϕ_i^1 can be constructed by matching together element shape functions $\hat{\phi}_1^0, \hat{\phi}_2^0, \hat{\phi}_1^1, \hat{\phi}_2^1$ and similarly $\phi_i(y)$ can be obtained by matching $\hat{\phi}_1$ and $\hat{\phi}_2$. In the Galerkin approximation, the same set of basis functions are used to approximate the test functions ϕ and ξ as are used for v and θ . Recalling that equations (33) and (34) must hold for arbitrary ϕ and ξ , we arrive at the following set of ordinary differential equations.

$$M \dot{v} = -F , \quad (37)$$

$$H \dot{\theta} = -T\theta + W . \quad (38)$$

Here

$$\underline{w} = \{v_1, \dot{v}_1, v_2, \dot{v}_2, \dots, v_N, \dot{v}_N\}^T,$$

$$\underline{\theta} = \{\theta_1, \theta_2, \dots, \theta_N\}^T,$$

$$\underline{F} = \{F_1, F_2, \dots, F_{2N}\}^T = \sum_{J=1}^{N-1} \{f_{JJ}, f_{(J+1)J}, f_{(J+3)J}\}^T,$$

$$f_{JJ} = \int_{\Omega_J} \left\{ \begin{array}{l} s \phi^0 \\ 1, y \end{array} + \sigma \phi^0 \\ \left. \begin{array}{l} 1, yy \\ 1, yy \end{array} \right\} \right. dy,$$

$$f_{(J+1)J} = \int_{\Omega_J} \left\{ \begin{array}{l} s \phi^1 \\ 1, y \end{array} + \sigma \phi^1 \\ \left. \begin{array}{l} 1, yy \\ 1, yy \end{array} \right\} \right. dy,$$

$$f_{(J+2)J} = \int_{\Omega_J} \left\{ \begin{array}{l} s \phi^0 \\ 2, y \end{array} + \sigma \phi^0 \\ \left. \begin{array}{l} 2, yy \\ 2, yy \end{array} \right\} \right. dy,$$

$$f_{(J+3)J} = \int_{\Omega_J} \left\{ \begin{array}{l} s \phi^1 \\ 2, y \end{array} + \sigma \phi^1 \\ \left. \begin{array}{l} 2, yy \\ 2, yy \end{array} \right\} \right. dy,$$

$$M = \sum_{J=1}^{N-1} \int_{\Omega_J} \left\{ \begin{array}{cccc} 0 & 0 & 1 & 0 \\ \phi & \phi & \phi & \phi \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 2 & 1 \\ 0 & 1 & 0 & 1 \\ \phi & \phi & \phi & \phi \\ 1 & 1 & 1 & 1 \\ 1 & 1 & 2 & 1 \\ 0 & 0 & 0 & 0 \\ \phi & \phi & \phi & \phi \\ 1 & 2 & 1 & 2 \\ 1 & 2 & 2 & 2 \\ 0 & 1 & 0 & 1 \\ \phi & \phi & \phi & \phi \\ 1 & 2 & 1 & 2 \\ 1 & 2 & 2 & 2 \end{array} \right\} dy,$$

with similar definitions for \underline{H} , \underline{T} and \underline{W} . In the above integrations Ω_J is the region occupied by the J th element. These integrals are evaluated numerically by using the 4-point Gauss integration rule. Explicit expressions for the matrices in Eq. (38) are not stated above since they are given in many books on the finite element method, e.g. Becker et al.⁷

Equations (37), (38), and (3)-(5) are integrated with respect to time t by using the simple forward-difference method. The solution of equations (37) and (38) gives nodal values of v , \dot{v} , and θ at the next step. From these, values of v_{yy} , \dot{v}_{yy} , and θ_{yy} at the Gauss points of integration are calculated by using the interpolation relations (35) and (36). For each Gauss point, Eqs. (3)-(5) are integrated to obtain the local values of s , σ , and ψ at the next time step. Because the integration scheme is only conditionally stable in the linear case, the time step has to be kept very small; its value is dependent on the grid size, the material properties, and the present deformations of the body.

C. Computation and Discussion of Results

In order to compute numerical results the following values of various non-dimensional parameters that correspond to a typical hard steel were chosen.

$$\rho = 3.928 \times 10^{-5}, \quad k = 3.978 \times 10^{-3}, \quad a = 0.4973, \quad \mu = 240.3, \\ n = 0.09, \quad \psi_0 = 0.017, \quad b = 5 \times 10^6, \quad m = 0.025.$$

For homogeneous deformations of the block, the peak in the shear stress-shear strain curve occurs at a strain of 0.093. The uniform temperature $\theta_0 = .1033$ in the block when $\gamma = 0.0692$ was perturbed by adding a smooth temperature bump

$$\tilde{\theta}(y) = 0.1 (1-y^2)^9 e^{-5y^2}$$

and the resulting initial-boundary value problem was solved by using the aforementioned two methods. In each case no attempt was made to use diagonal matrices equivalent, in some sense, to those computed by using the basis functions. The domain $[0, 1]$ was divided into 13 subdomains with nodes at 0, .05, .10, .15, .20, .25, .34375, .43750, .53120, .6250, .71875, .81250, 1.0. For the forward-difference scheme various integrals appearing in the expressions for F , M , H , T and W were evaluated by using the 4-point Gauss quadrature rule.

When $\epsilon = 0.0$ and 0.01 , the forward-difference scheme necessitated taking $\Delta t = .5 \times 10^{-7}$ in order to obtain a stable solution. However, for the Crank-Nicolson method, $\Delta t = .1 \times 10^{-4}$ was found to give a stable and acceptable solution since the results obtained with $\Delta t = .5 \times 10^{-5}$ were found to be indistinguishable from those computed with the larger value of Δt . As is clear from the two sets of results shown in Figs. 1 and 2, the non-physical damping introduced by the Crank-Nicolson method results in the delayed response as compared to that obtained with the forward-difference method. As is discussed in Reference 6, the development of a late stage plateau is a numerical artifact and does not represent a physical phenomenon. The plateau was also developed in the solution computed by using the forward-difference method even though it is not depicted in the figure.

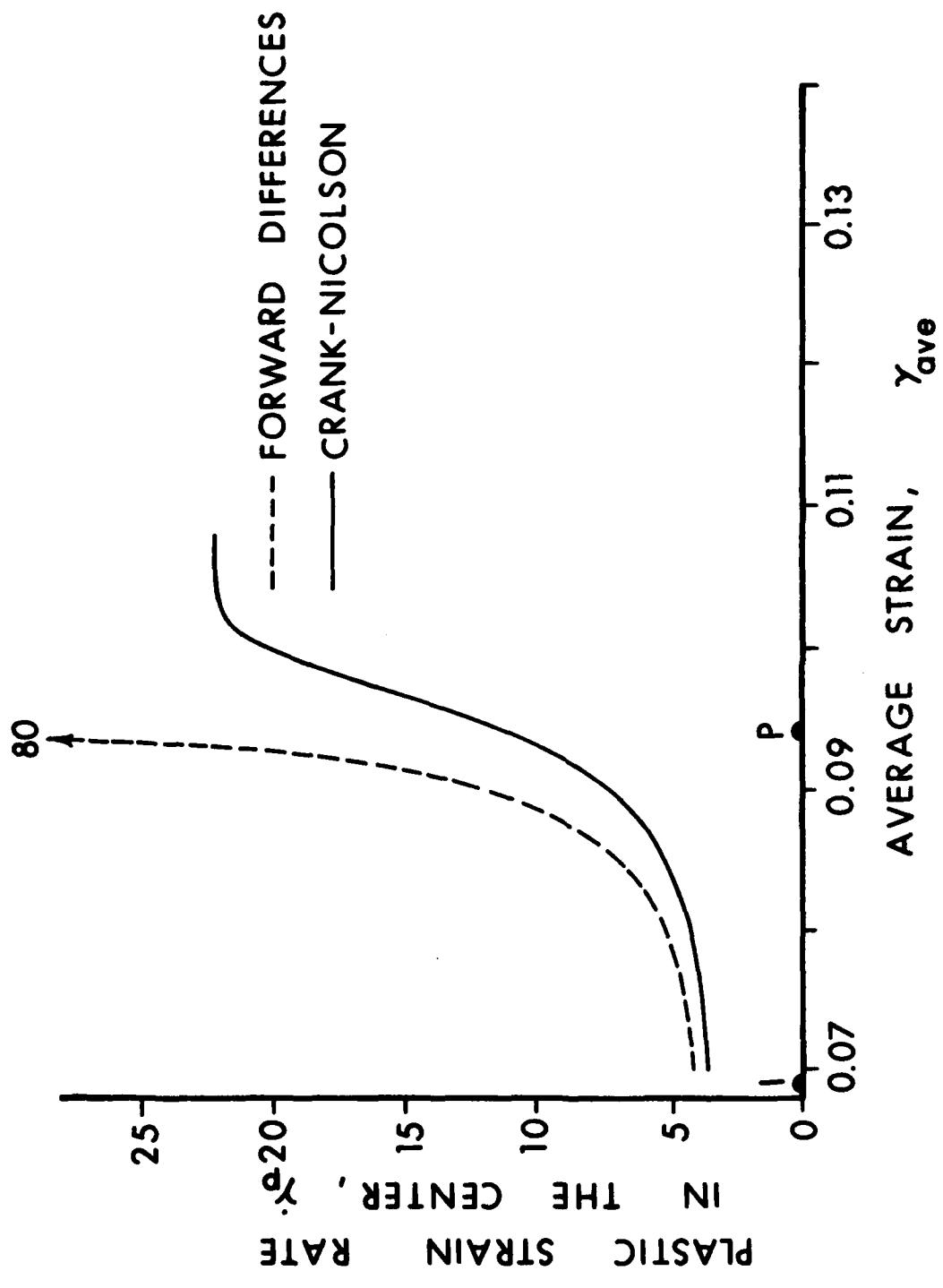


Figure 1: Comparison of Solutions (for $\lambda = 0.0$) by the Two Different Integration Techniques.

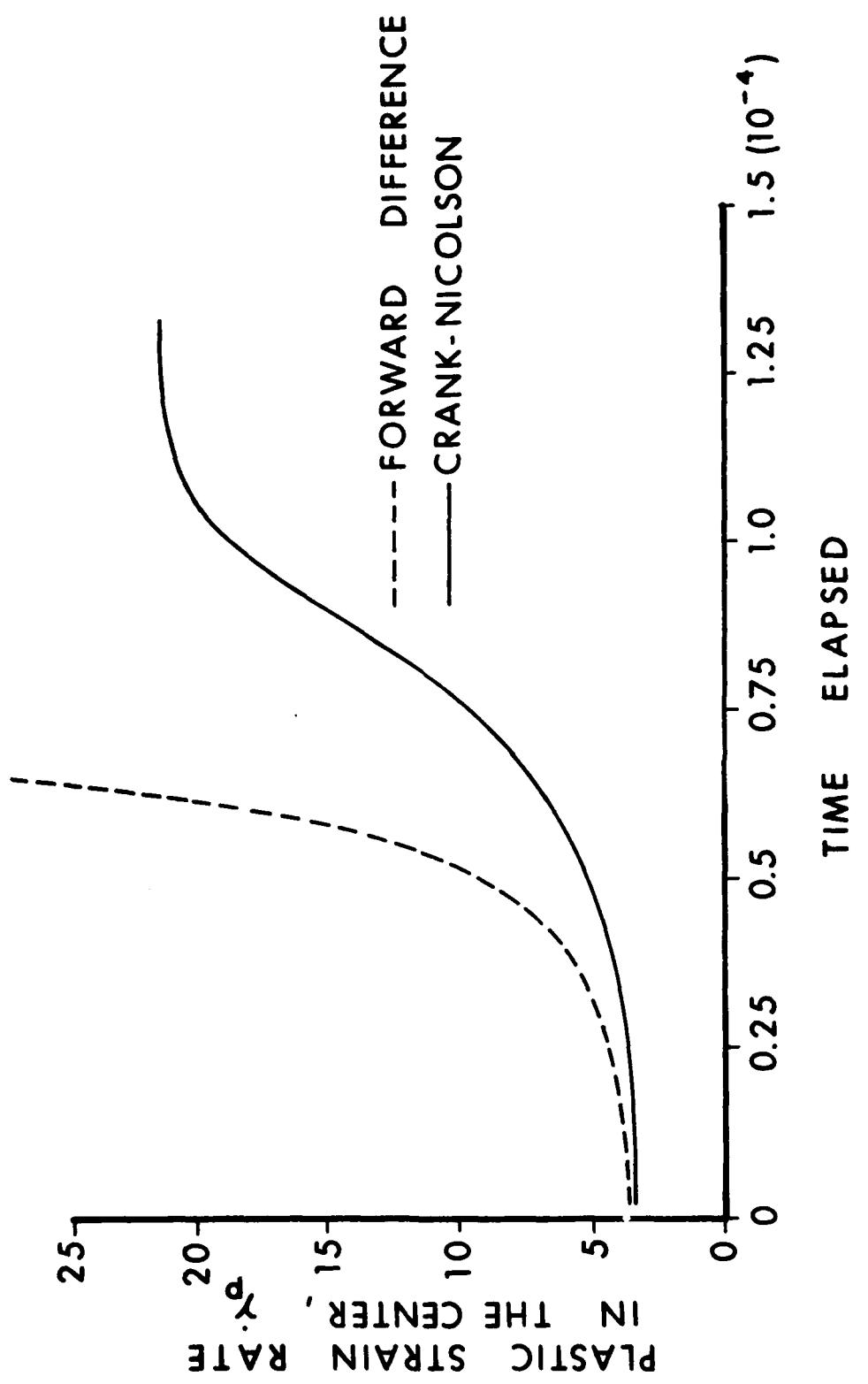


Figure 2: Comparison of Solutions (for $\lambda = 0.01$) by the Two Different Integration Techniques.

The spatial variation of s at late times also indicates some kind of numerical instability. Since the average applied strain rate is unity, the abscissa also represents the time measured from the instant (denoted by I in Fig. 1) the uniform temperature field is perturbed. On an IBM 4381 computer, the CPU time required to compute the solution by the finite-difference method was nearly three times that needed for the other method when ϵ in Eqn. (32) was set equal to .01.

Figures 3 and 4 compare the solutions for $\ell = 0.0$ and $\ell = 0.01$ obtained by the Crank-Nicolson method and the forward-difference method. In each case, $\ell = 0.01$ results in a delayed response in the sense that $\dot{\gamma}_p(0,t)$

begins to rise to its maximum value slower and later. However, the two integration techniques depict a similar qualitative difference between the solutions of governing equations for $\ell = 0.0$ and $\ell = 0.01$. We have plotted only $\dot{\gamma}_p(0,t)$ versus t in all of the figures since the $\dot{\gamma}_p(y,t)$ is maximum at $y=0$ and the rate at which $\dot{\gamma}_p(0,t)$ builds up is important in physical problems. The evolution in time of other variables, the spatial variation of these variables at different times, as well as the effect of choosing different perturbations $\theta(y)$ have been given in [6,8,9].

Whether or not the introduction of auxiliary variables in the FDGFE method will permit the use of a larger time step remains to be seen. Also, the use of automatic time-step control as discussed by Chandra and Mukherjee⁵ may improve the efficiency of the FDGFE method. Further work in resolving some of the issues raised herein and selecting an optimum value of Δt is currently under progress and will be reported on in future.

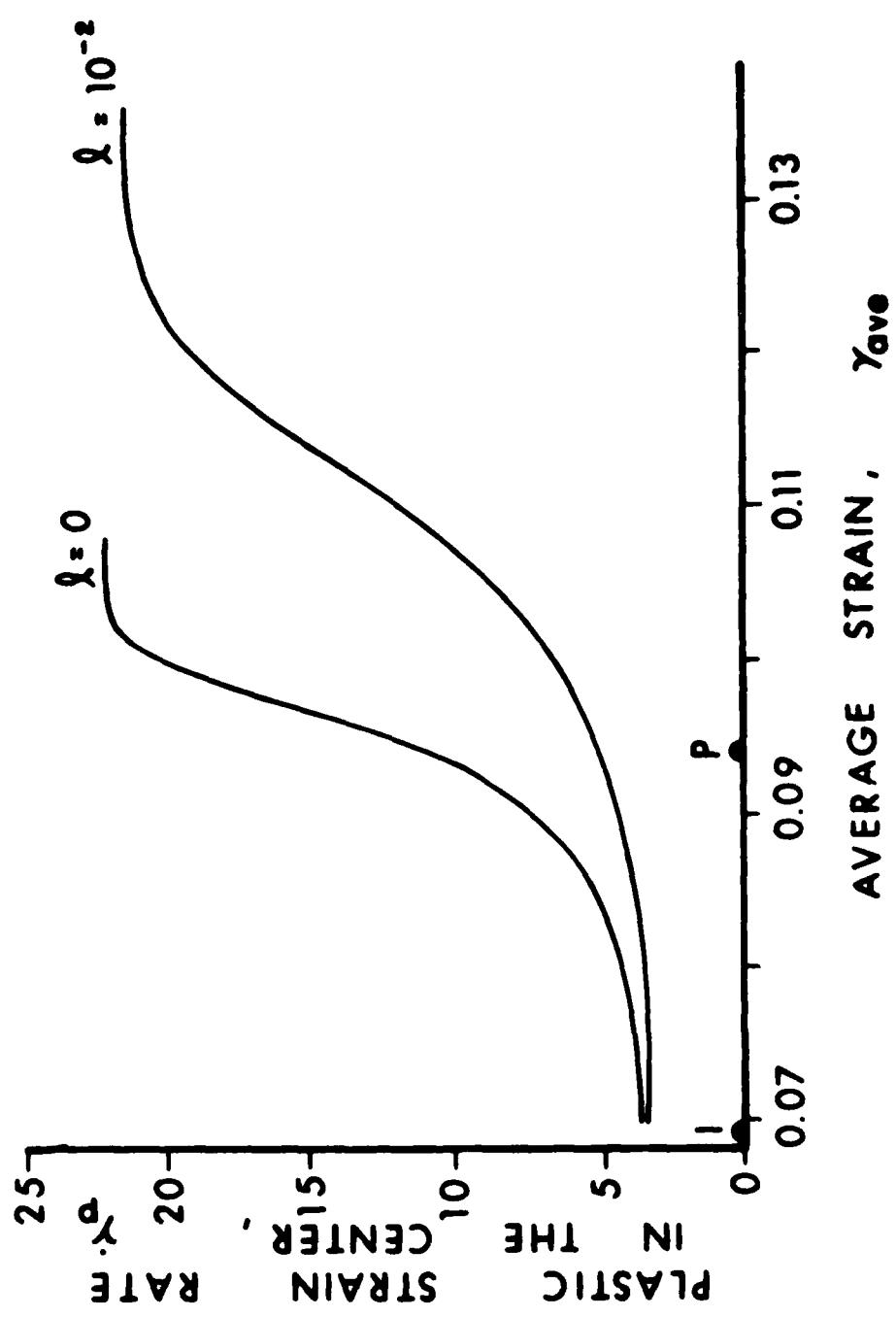


Figure 3: Comparison of Solutions for $\delta = 0.0$ and $\delta = 0.01$ by the CNGFE Method.

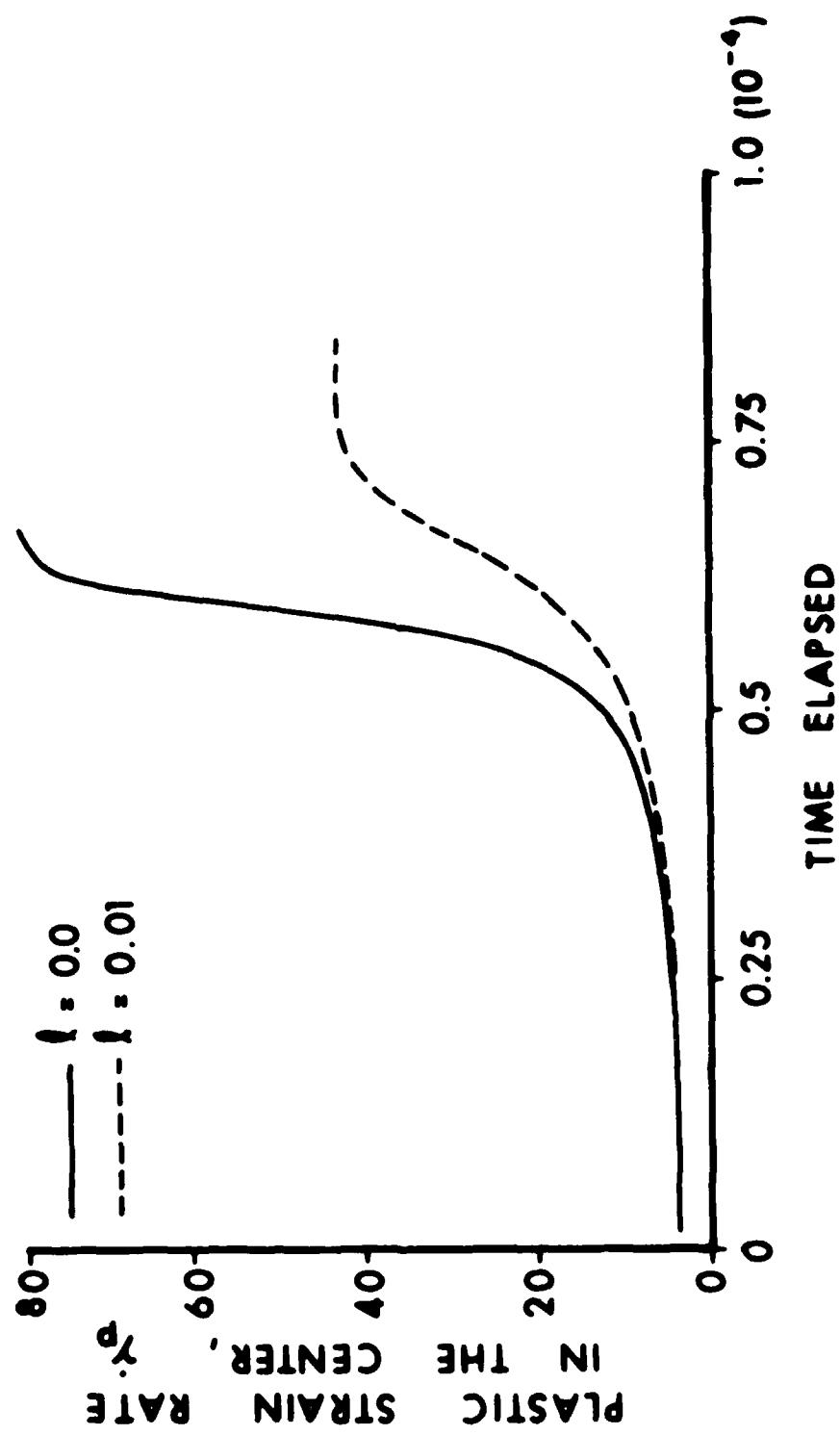


Figure 4: Comparison of Solutions for $t = 0.0$ and $t = 0.01$ by the FDGFE Method.

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APPENDIX
CODE LISTING

```

PROGRAM ADIAB(IINPUT,JINPUT,TAPE5=IINPUT,TAPE6=JINPUT)
DIME'IS'IN YCORD(30),NODE(2,30), EMASS(10),AMASS(4,42)
+ ,FORCE(62),EFORCE(4), TGDDT(31)
DIMENSION LD(4),ETAU(5),YY(2),ESIG(5), WORK(5,30)
+ ,VELDDT(31), DDODT(5,30), SIGMA(5,30)
+ ,PGDDT(5,30),PDODT(5,30),EGDDT(5,30),TEMP(5,30)
+ ,PGAMA(5,100),SI(5,100),TMP(31),PD(5,100),TAU(5,30)
C
C
C      READ THE INPUT DATA
C
READ(5,1000) C4,CN,BETA,A,B,SIO,RHO,CV
READ(5,1010) NT,NINT,DT,CK,CJ,GDDT0,CNU,CNU
READ(5,1020) NUMEL,NODES,NPRINT,CL,HT
READ(5,1025) TIME,RSTART
CNU=C NU*1000.
C
C
1000 FORMAT(8F10.4)
1010 FORMAT(1T,I3,6F10.4)
1020 FORMAT(3I5,2F10.5)
1025 FORMAT(E10.4,F10.4)
C
C      PRINT OUT THE INPUT DATA.
C
WRITE(6,2000) C4,CN,BETA,A,B,SIO,RHO,CV
WRITE(6,2010) NT,NINT,DT,CK,CJ,GDDT0,CNU,CNU
WRITE(6,2020) NUMEL,NODES,CL,HT,NPRINT
WRITE(6,2025) TIME,RSTART
C
C
C      GENERATE NODE NUMBERS AND NON-DIMENSIONAL COORDINATES.
C
CALL GRID(YCORD,NODE,NODES,NUMEL )
C
C
C      PRINT OUT THE NON-DIMENSIONAL MODAL COORDINATES.
C
DO 35 J=1,NODES
35 WRITE(6,2030) J,YCORD(J)
DO 40 I=1,NUMEL
40 WRITE(6,2040) I,NODE(1,I),NODE(2,I),
2000 FORMAT(5X,'H=' ,E15.5/5X,'N=' ,E15.5/5X,'BETA=' ,E15.5/
+ 5X,'A=' ,E15.5/5X,'B=' ,E15.5/5X,'SIO=' ,E15.5/
+ 5X,'RHO=' ,E15.5/5X,'CV=' ,E15.5)
2010 FORMAT(5X,'NO. OF TIME STEPS =',I10/
+ 5X,'NO. OF INTEG. POINTS USED IN NUMERICAL INTEGRATION =',I5/
+ 5X,'TIME INCREMENT =',E15.5/
+ 5X,'THERMAL CONDUCTIVITY =',E15.5/5X
+ ,,'FACTOR TO CONVERT FROM JOULES TO KG-M =',E15.5/
+ 5X,'PRESCRIBED STRAIN RATE =',E15.5/5X,'W = ',E15.5/
+ 5X,'NU = ',E15.5)
2020 FORMAT(5X,'NUMBER OF ELEMENTS =',I10/5X,
+ 'NUMBER OF NODES =',I10
+ /5X,'MATERIAL LENGTH = ',E15.5/5X,
+ 'HEIGHT OF THE SPECIMEN (H IN METERS ) = ',E15.5
+ /5X,'PRINT INTERVAL = ',I5)
2025 FORMAT(5X,'TIME AT THE START OF THIS RUN =',E15.5/5X,
+ 'RESTART JOB IF RSTART = 0.0; OTHERWISE NOT A',1X,
+ 'RESTART JOB.'/5X,'RSTART = ',F15.5)
C
C
C      COMPUTE NON-DIMENSIONAL NUMBERS
C
CKAPAD = BETA*(SIO**CNU)

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      A = A*TR                               000760
      FACT1 = 4.0*CK/(HT+HT*RHO*CV*G0)TO)   000770
      FACTL = 2.*CL/HT                         000780
      RHO = RHO*((HT*G0)TO/2.)*2)/CKAPAO     000790
      RHOI=1.0/RHO                            000800
      CMU = CMU/CKAPAO                        000805
      CMU1 = CMU*2./(CKAPAO+HT*CL)            000810
      WRITE(6,2055) CKAPAO,FACT1,RHO,CMU,CMU1,A,TR    000820
2055 FORMAT(5X,'KAPAO = ',E15.5/5X,'THERMAL FACTOR = ',E15.5/5X,
      *'INERTIA FACTOR = ',E15.5/5X,'NUBAR = ',E15.5/5X,
      *'NU-TAR = ',E15.5/5X,'NDIM-DIMENSIONAL A = ',E15.5
      *'/5X,'REFERENCE TEMPERATURE = ',E15.5)        000830
      2050 FORMAT(5X,I5,F15.5)                  000840
      2040 FORMAT(5X,3I10)                      000850
C
C      READ THE PARAMETERS CONTROLLING THE DISTURBANCE.          000860
C
      READ(5,1000) ALFA,CNN,EPISILON           000870
      READ(5,1030) HTAU,4GP,HSI,HGPDOT,HT4P,4GT   000880
C      READ (9,1031) TIME,HTAU,4GP,-4T,HT4P,HSI,HGPDOT 000890
C1031 FORMAT(50X,E20.10/10X,E20.10/24X,E20.10/?3X,E20.10/
      *23X,E20.10/14X,E23.10/3JX,E20.10)           000900
C      WRITE(6,2031) HTAU,4GP,4GT,HT4P,HSI,HGPDOT 000910
      WRITE(6,2050) ALFA,CNN,EPISILON           000920
      2050 FORMAT(5X,'VALUES OF VARIABLES CONTROLLING THE DISTURBANCE'/
      *5X,'ALFA = ',E15.5/5X,'N = ',E15.5/5X,'EPISILON = ',E15.5) 000930
C
C      GENERATE VALUES OF SHAPE FUNCTIONS AND THEIR DERIVATIVES. 000940
C
C      CALL SHAPES (INT)                           000950
C
C      CALCULATE VALUES OF GAMMA-DOT AND D-DOT CAUSED BY      000960
      THE INITIAL DISTURBANCE.                          000970
C
      IFIRSTART,NE,0.0)
      *CALL DISTURB(TC)RD,NODE,EGDDOT,DDDDOT, ALFA,CNN, EPISILON 000980
      *,NUREL,MINT,TE4P,T4P,NIDES,NT4P )             000990
C
C      CALCULATE THE INITIAL YIELD STRESS.                 001000
      CK = ((1.0+CSI/S10)*CNN)*(1.0+B*GDDOT*HGPDOT)*CNN 001010
C
C      TAU0 = TAU0/CKAPAO.                            001020
C
      TAU0 = HTAU                                     001030
C
C      SET INITIAL STRESS = YIELD STRESS. THE INITIAL DISTURBANCE ALTERS 001040
      THE TOTAL STRAIN RATE AT A NODE POINT.          001050
C
C      SET THE INITIAL STRAIN RATE = STRAIN RATE DUE TO HOMOGENEOUS 001060
      DEFORMATION + STRAIN RATE CAUSED BY THE DISTURBANCE. 001070
C      NON-DIMENSIONALIZED STRAIN RATE DUE TO HOMOGENEOUS DEFORMATION 001080
      IS EQUAL TO 1.0.                                001090
C
      IFIRSTART,EQ,0.0) GO TO 99
      M1 45 NEL = 1, NUREL
      DD 45 INT = 1, NT4P
      EGDDOT(INT,NEL) = EGDDOT(INT,NEL) + 1.0
45  CONTINUE
C      SET INITIAL STRESS = STRESS CAUSED BY THE DISTURBANCE + TAU0 001100
      STRESSES CAUSED BY THE DISTURBANCE ARE TAKEN EQUAL TO 0 001110
C
      M1 46 I = 1,NUREL
      DD 46 J = 1,NT4P

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TR = CKAPAO/(PHI*CV*CJ)          000760
A = A+TR                         000770
FACT1 = 4.0*CK/(HT*HT*RHO*CV*G0)TO 000780
FACL = 2.*CL/HT                  000790
RHO = RHO*((HT*G0)TO/2.)**2)/CKAPAO 000800
RHOI=1.0/RHO                      0008C5
CMU = CMU/CKAPAO                 000910
CNU = CNU*2.0/(CKAPAO*HT*CL)      000820
WRITE(6,2035) CKAPAO,FACT1,RHO,CMU,CNU,A,TR 000830
2055 FORMAT(5X,'KAPAO = ',E15.5/5X,'THERMAL FACTOR = ',E15.5/5X,
    + 'INERTIA FACTOR = ',E15.5/5X,'MUSAR = ',E15.5/5X,
    + 'MU-TAR = ',E15.5/5X,'NON-DIMENSIONAL A = ',E15.5
    + '/5X,'REFERENCE TEMPERATURE = ',E15.5)
2030 FORMAT(5X,I5,F15.5)
2040 FORMAT(5X,3I10)
C
C      READ THE PARAMETERS CONTROLLING THE DISTURBANCE.
C
C      READ(5,1009) ALFA,CHN,EPISILON
C      READ(5,1030) HTAU,HGP,HSI,HGPDT,HTMP,HGT
C      READ(5,1031) TIME,HTAU,HGP,-HT,HTMP,HSI,HGPDT
C1731 FORMAT(5X,E20.10/10X,E20.10/24X,E20.10/?3X,E20.10/
    + 23X,E20.10/14X,E20.10/3JX,E20.10)
C      WRITE(6,2031) HTAU,HGP,HSI,HTMP,HGT,HGPDT
C      WRITE(6,2050) ALFA,CHN,EPISILON
2050 FORMAT(5X,'VALUES OF VARIABLES CONTROLLING THE DISTURBANCE'/
    + ' ',E15.5/5X,'N = ',E15.5/5X,'EPISILON = ',E15.5)
C
C      GENERATE VALUES OF SHAPE FUNCTIONS AND THEIR DERIVATIVES.
C
C      CALL SHAPES (NINT)
C
C      CALCULATE VALUES OF GAMMA-DOT AND D-DOT CAUSED BY
C      THE INITIAL DISTURBANCE.
C
C      IF(RSTART.NE.0.0)
C      +CALL DISTUBP(YCJRD,NODE,EGD0T,DD00T, ALFA,CHN, EPISILON
C      + ,NHEMEL,NINT,TE1P,TMP,NHDES,HTMP )
C
C      CALCULATE THE INITIAL YIELD STRESS.
C      CK = ((1.0+HSI/S10)**CH)*(1.0+9*G0*HGPDT)**CH
C
C      TAU0 = TAU0/CKAPAO.
C
C      TAU0 = HTAU
C
C      SET INITIAL STRESS = YIELD STRESS. THE INITIAL DISTURBANCE ALTERS
C      THE TOTAL STRAIN RATE AT A NODE POINT.
C
C      SET THE INITIAL STRAIN RATE = STRAIN RATE DUE TO HOMOGENEOUS
C      DEFORMATION + STRAIN RATE CAUSED BY THE DISTURBANCE.
C      NON-DIMENSIONALIZED STRAIN RATE DUE TO HOMOGENEOUS DEFORMATION
C      IS EQUAL TO 1.0
C
C      IF(RSTART.EQ.0.0) GO TO 95
C      DO 45 NEL = 1, NHEMEL
C      DO 45 INT = 1, NINT
C      EGD0T(INT,NEL) = EGD0T(INT,NEL) + 1.0
45  CONTINUE
C      SET INITIAL STRESS = STRESS CAUSED BY THE DISTURBANCE + TAU0
C      STRESSES CAUSED BY THE DISTURBANCE ARE TAKEN EQUAL TO 0
C
C      DO 46 I = 1,NHEMEL
C      DO 46 J = 1,NINT

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      SIGMA(J,I) = 0.0          001320
  46   TAU(J,I) = CK*(1.0-A*TEMP(J,I)) 001320
  55   CONTINUE                 001331
C     FOR THE RESTART JOB, READ VELOCITY,TEMP,SI,TAU,SIGMA.
  IF(RSTART.NE.0.0) GO TO 70 001332
  DO 60 NEL = 1,NUMEL        001333
  DO 60 INT = 1,4INT        001334
  READ(5,1070) TAU(INT,NEL),SIGMA(INT,NEL),PGAMA(INT,NEL) 001335
  READ(5,1071) SI(INT,NEL),PGDOT(INT,NEL),TEMP(INT,NEL),PD(INT,NEL) 001336
  READ(5,1072) EGDOT(INT,NEL),DDODOT(INT,NEL)            001337
  60   CONTINUE                 001338
  1070 FORMAT(10X,3E20.12)      001339
  1071 FORMAT(2X,4E19.12)       001340
  1072 FORMAT(2X,2E19.12)       001341
  DO 65 NOD = 1, NODES       001342
  65   READ(5,1073) VELDOT(NOD),TGDOT(NOD),TMRP(NOD)      001343
  1073 FORMAT(15X,3E15.7)       001344
  CALL DD(DDODOT,NINT,NUMEL,NODE,VELDOT,TGDT,YCORD,EGDOT,DT,NZERO,
+NTT)                         001345
  70   CONTINUE                 001346
  CM=1./CM                      001347
  GDDOTI = 1.0/GD0TO           001348
C
C
  1030 FORMAT(6F10.4)          001349
  WRITE(6,2031) 4TAU,HGP,HSI,HGPDOT,HTMP,HGT             001350
  2031 FORMAT(5X,'HTA' = ',E15.5/5X,'HGP = ',E15.5/5X,'HSE = ',E15.5/
+ 5X,'HGPDOT = ',E15.5/5X,'HTMP = ',E15.5/5X,'HGT = ',E15.5) 001351
C
  NDF=2*NODES                  001352
  MB=4                          001353
  DO 990 NTT=1,NT               001354
C
C     INITIALIZE THE GLOBAL MASS MATRIX AND THE GLOBAL FORCE VECTOR. 001355
C     THE MASS MATRIX IS GENERALIZED IN THE SENSE THAT IT INCLUDES 001356
C     THE INERTIA TERMS APPROPRIATE FOR D-DOUBLE DOT. THE FORCE VECTOR 001357
C     EQUALS THE RESULTANT OF FORCES CAUSED BY STRESSES AND 001358
C     DIPOLEAR STRESSES DUE TO THE DISTURBANCE. 001359
C
  DO 50 I=1,NDF                001360
  FORCE(I)=0.0                  001361
  IF(NTT.NE.1) GO TO 50          001362
  DO 49 J=1,MB                  001363
  49   AMASS(J,I) = 0.0          001364
  50   CONTINUE                  001365
C
C     TIME = TIME + DT*GD0TOI    001366
C
  NCOUNT = NTT/NPRINT           001367
  NZERO = NCOUNT * NPRINT - NTT 001368
C     FIND THE HYDROGENETUS SOLUTION FOR THE PRESENT VALUE OF TIME. 001369
C
  CALL 1070G('HTMP,HGT,HGP',ITA',HSI,CM,CH,A,B,GPROTO
+ ,CM,DT,SIO,TIME, HGPDOT,NZERO) 001370
C
C     ASSEMBLE THE GLOBAL MASS MATRIX. 001371
C
  DO 900 NELM=1,NUMEL          001372
  DO 100 I=1,2                  001373
  II=NODE(I,NELM)              001374
  YY(I) = YCORD(II)             001375
  100 CONTINUE                  001376

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      DO 105 INT = 1, NINT          001820
      ETAU(INT) = TAU(INT,NELM)      001830
105  ESIG(INT) = SIGMA(INT,NELM)  001840
C
C   CALCULATE THE ELEMENT MASS MATRIX AND THE FORCE VECTOR 001850
C
      CALL ELEMENT(YY,ETAU,ESIG,EFORCE,EMASS,NINT,FACL,NTT) 001860
      DO 110 II=1,2                 001870
      JJ=2*II                      001880
      I = NODE(II,NELM)*2           001890
      LD(JJ-1)=I-1                  001900
110  LD(JJ)=I                     001910
      MC=0                          001920
      DO 130 II=1,4                 001930
      I=LD(II)                      001940
      FORCE(I) = FORCE(I) + EFORCE(II) 001950
      IF(NTT,NE,1) G7 TO 130         001960
      DO 120 JJ=1,II                 001970
      MC=MC+1                       001980
      M=LD(JJ)                      001990
      IR=MINO(I,M)                  002000
      IC=IABS(I-M)+1                002010
120  AMASS(IC,IR)=AMASS(IC,IR)+EMASS(MC) 002020
130  CONTINUE                      002030
130  CONTINUE                      002040
130  CONTINUE                      002050
      DO 915 J=1,NDF               002060
      FORCE(J) = FORCE(J)*RHOJ     002070
915  CONTINUE                      002080
C
C   MODIFY THE MASS MATRIX FOR THE PRESCRIBED BOUNDARY CONDITIONS. 002085
C
C   AT THE BOUNDARY NODES (THE FIRST AND THE LAST NODE) 002090
      GAMMA AND VELOCITY IS PRESCRIBED. 002100
C   THEREFORE, WE SET GAMMA - DOUBLE-DOT = 0.0 AND ACCELERATION = 0.0 002110
      AT THESE NODES. 002120
C
      II = 2*NODES-1              002130
      CALL MODIFY(1,0.0,AMASS,FORCE,NDF,MB,MB) 002140
      CALL MODIFY(II,0.0,AMASS,FORCE,NDF,MB,MB) 002150
      IF(NTT,EQ,1)                  002160
      +CALL SOLVE(AMASS,FORCE,NDF,MB,MB,1) 002170
      CALL SOLVE(AMASS,FORCE,NDF,MB,MB,2) 002180
C
C
      NOW THE ARRAY FORCE CONTAINS TOTAL MODAL ACCELERATIONS AND MODAL 002190
      STRAIN DOUBLE-DOTS CAUSED BY THE DISTURBANCE. FROM THESE VALUES FIND 002200
      VALUES OF DDDOT. 002210
C
C   TRANSFER VALUES FROM THE ARRAY FORCE INT ARRAYS VELDOT AND DDDOT. 002220
C
2110 FORMAT(5X,'ACCELERATION DUE TO DISTURBANCE AND TOTAL GAMMA-2 DOT' / 002230
      + 5X,'NODE #',5X,'ACCELERATION',5X,'GAMA-DOUBLE DOT') 002240
      DO 200 I = 1, NODES          002250
      II = 2*I                      002260
      VELDOT(I) = FORCE(II-1)        002270
      TDDOT(I) = FORCE(II)          002280
2100 FORMAT(5X,I5,2E15.9)        002290
200  CONTINUE                      002300
C
C   FIND PLASTIC PARTS OF EDDOT AND DDDOT. DENOTE THESE 002310
      BY PGDDOT,PDDDOT. 002320
C
C

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CALL PLASTIC(EGDOT,DDDOT,PGDGT,PGDT, CHI,GDGT0,SIGMA, CN,  

+ A,B,CMU,CHI,DT,TAU0,TEMP,SIO, NTT,NUMEL,NINT,WORK,TAU  

+ ,HSI,HGP,HGPDOT,PGAMA,SI,RSTART,PD) 002550  

002560  

002561  

002570  

C CALCULATE TOTAL DDOT AND TOTAL GDOT. 002571  

CALL DD(DDDT,NINT,NUMEL,NODE,VELDOT,TGDOT,YCORD,EGDOT,DT,NZERO,  

+ NTT) 002572  

002573  

C  

CCC SOLVE THE THERMAL PROBLEM 002620  

002630  

C CALL THERM(TEMP,WORK,FACT1, NUMEL,NINT,NTT,DT,TMP  

+ ,YC0RD,NODES,NODE) 002640  

002650  

IF(NZERO. NE. 0) GO TO 990 002661  

DO 985 NEL = 1,NUMEL 002680  

DO 983 INT = 1, NINT 002690  

WRITE(6,2400) NEL,INT,TAU(INT,NEL),SIGMA(INT,NEL),PGAMA(INT,NEL) 002691  

WRITE(6,2401) SI(INT,NEL),PGDGT(INT,NEL),TEMP(INT,NEL),PD(INT,NEL) 002692  

WRITE(6,2401) EGDOT(INT,NEL),DDDOT(INT,NEL) 002693  

985 CONTINUE 002694  

DO 980 NOD=1,NODES 002695  

980 WRITE(6,2290) NOD,VELDOT(NOD),TGDOT(NOD),TMP(NOD) 002696  

2290 F0R4MAT(10X,I5,3E15.7) 002697  

2400 FORMAT(2X,2I4,3E20.12) 002698  

2401 FORMAT(2X,4E19.12) 002699  

990 CONTINUE 002730  

STOP 002740  

END 002750  

SUBROUTINE HOMOG(HTMP,HGT,HGP,HTAU,HSI,CMU, CN,A,B,GGDGT  

+ , CMU,DT,SIO,TIME, HGPDOT,NZERO) 002760  

HCKAPA1 = (1.0 + HSI/SIO)**CHI 002770  

HCKAPA = HCKAPA1 * (1.0 - A * HTMP) 002780  

QT=HTAU/HCKAPA 002800  

IF(QT.LT.1.0)GO TO 500 002810  

R2=QT**CHI - 1.0 002830  

GAMA = R2/(B*GGDGT *HTAU) 002840  

GO TO 600 002850  

500 WRITE(6,2000) QT,TIME 002860  

GAMA = 0.0 002870  

600 CONTINUE 002880  

HSIDOT = GAMA*(HTAU*HTAU/HCKAPA1) 002890  

HGPDT = GAMA * HTAU 002900  

HTMPDT = HGPDOT * HTAU 002910  

HTAUDT=CMU*(1.0-HGPDOT) 002920  

HSI=HSI+HSIDOT*DT 002930  

HTAU=HTAU+HTAUDT*DT 002940  

HGP=HGP+HGPDOT*DT 002950  

HGT=HGT+ DT 002960  

HTMP = HTMP + HTMPDT*DT 002970  

IF(NZERO.EQ.0)WRITE(6,2005) TIME,HTAU,HGP,HGT,HTMP,HSI,HGPDOT 002980  

2005 FORMAT(5X,'HOMOGENEOUS SOLN. AT PHYSICAL TIME (SECS.) =',E20.10/  

+ 5X,'TAU = ',E20.10/5X,'GA/IA -PLASTIC = ',E20.10/  

+ 5X,'TOTAL STRAIN = ',E20.10/5X,'TEMPERATURE = ',E20.10/  

+ 5X,'SI = ',E20.10 003000  

+ /5X,'PLASTIC STRAIN-RATE = ',E20.10) 003010  

003020  

003021  

RETURN 003030  

2000 FORMAT(5X,'FOR THE HOMOG. SOLN. THE MATERIAL IS DEFORMING'  

+ ,1X,'ELASTICALLY',  

+ 5X,'RATIO OF STRESS TO HARDEMING FUNCTION = ',F15.5/  

+ 5X,'CURRENT VALUE OF TIME = ',F15.5)  

END 003040  

SUBROUTINE SHAPES(NINT)  

COMMON//SHAPES/SHAPO(2,5),SHAP1(2,5),DSHAPO(2,5),DSHAP1(2,5),  

+ DDSHAPO(2,5),DDSHAP1(2,5),SHAPB(2,5),DSHAPB(2,5) 003050  

003060  

003070  

003080  

003090  

003100  

003110

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DIME'ISITM SI(4)          003130
SI(1) = -0.861136311594053 003160
SI(2) = -0.339781043584856 003170
SI(3) = - SI(2)            003190
SI(4) = - SI(1)            003200
C
C EVALUATE THE SHAPE FUNCTIONS AND THEIR DERIVATIVES.
C
DO 100 I = 1,NINT          003210
S=SI(I)                    003220
SHAP0(1,I) = (2.0 - 3.0*S + S**3)/4.0 003230
SHAP0(2,I) = (2.0 + 3.0*S - S**3)/4.0 003240
SHAP1(1,I) = (1.0 - S - S*S + S**3)/4.0 003250
SHAP1(2,I) = (-1.0 - S + S*S + S**3)/4.0 003260
DSHAP0(1,I) = (-3.0 + 3.0*S*S)/4.0 003270
DSHAP0(2,I) = (3.0 - 3.0*S*S)/4.0 003280
DSHAP1(1,I) = (-1.0 - 2.0*S + 3.0*S*S)/4.0 003290
DSHAP1(2,I) = (-1.0 + 2.0*S + 3.0*S*S)/4.0 003300
DDSHAP0(1,I) = (6.0*S)/4.0 003310
DDSHAP0(2,I) = (-6.0*S)/4.0 003320
DDSHAP1(1,I) = (-2.0+6.0*S)/4.0 003330
DDSHAP1(2,I) = ( 2.0 + 6.0*S)/4.0 003340
C
SHAPB(1,I) = (1.0 - S)/2.0 003350
SHAPB(2,I) = (1.0 + S)/2.0 003360
DSHAPB(1,I) = -1./2. 003370
DSHAPB(2,I) = 1./2. 003380
C
100 CONTINUE
RETURN
END
SUBROUTINE ELEMENT(YY,ETAU,ESIG,EFORCE,EMASS,NINT,FACTL,NTT)
COMMON/SHAPES/SHAP0(2,5),SHAP1(2,5),DSHAP0(2,5),DSHAP1(2,5),
+ DDSHAP0(2,5),DDSHAP1(2,5),SHAPB(2,5),DSHAPB(2,5)
DIMENSION YY(2),ETAU(5),WEIGHT(5),EFORCE(4),EMASS(10),ESIG(5)
WEIGHT(1) = 0.347854845137434 003390
WEIGHT(2) = 0.652145154962546 003400
WEIGHT(3) = WEIGHT(2) 003410
WEIGHT(4) = WEIGHT(1) 003420
MC=0 003430
C
DO 100 I = 1,4 003440
EFORCE(I) = 0.0 003450
IF(NTT.NE.1) GO TO 100 003460
DO 50 J= 1, I 003470
MC=MC+1 003480
50 EMASS(MC)=0.0 003490
100 CONTINUE 003500
DO 200 INT = 1,NINT 003510
WT=WEIGHT(INT) 003520
DJAC = (YY(2) - YY(1))*0.50 003530
C
WRITE(6,2010) DJAC 003540
2010 FORMAT(5X,'DJAC = ',E15.5) 003550
IF(NTT.NE.1) GO TO 185 003560
ST2 = WT*DJAC 003570
EMASS(1) = EMASS(1) + SHAP0(1,INT)*SHAP0(1,INT)*ST2 003580
EMASS(2) = EMASS(2) + SHAP0(1,INT)*SHAP1(1,INT)*ST2 003590
EMASS(3) = EMASS(3) + SHAP1(1,INT)*SHAP1(1,INT)*ST2 003600
EMASS(4) = EMASS(4) + SHAP0(1,INT)*SHAP0(2,INT)*ST2 003610
EMASS(5) = EMASS(5) + SHAP1(1,INT)*SHAP0(2,INT)*ST2 003620
EMASS(6) = EMASS(6) + SHAP0(2,INT)*SHAP0(2,INT)*ST2 003630
EMASS(7) = EMASS(7) + SHAP0(1,INT)*SHAP1(2,INT)*ST2 003640
EMASS(8) = EMASS(8) + SHAP1(1,INT)*SHAP1(2,INT)*ST2 003650
EMASS(9) = EMASS(9) + SHAP0(2,INT)*SHAP1(2,INT)*ST2 003660

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185 EMASS(10)= EMASS(10)+ SHAP1(2,INT)*SHAP1(2,INT)*ST2      004050
CONTINUE
IF(DJAC.LE.1.0E-20) GO TO 3000
WT1=WT*FACT/DJAC
GO T1 190
004060
004070
004080
004090
004100
004110
004120
004130
3000 WRITE(6,2020) DJAC
2020 FORMAT(5X,'DJAC = ',E15.5)
STOP
004140
190 CONTINUE
EFORCE(1) = EFORCE(1) - (ETAU(INT)*DSHAP0(1,INT)*WT +
+ ESIG(INT)*DDSHAP0(1,INT)*WT1)                         C04150
EFORCE(2) = EFORCE(2) - (ETAU(INT)*DSHAP1(1,INT)*WT +
+ ESIG(INT)*DDSHAP1(1,INT)*WT1)                         CC4160
EFORCE(3) = EFORCE(3) - (ETAU(INT)*DSHAP0(2,INT)*WT +
+ ESIG(INT)*DDSHAP0(2,INT)*WT1)                         CC4170
EFORCE(4) = EFORCE(4) - (ETAU(INT)*DSHAP1(2,INT)*WT +
+ ESIG(INT)*DDSHAP1(2,INT)*WT1)                         CC4180
004190
004200
004210
004220
200 CONTINUE
004230
C
C   WRITE(6,2030) EFORCE(1),EFORCE(2),EFORCE(3),EFORCE(4) 004240
2030 FORMAT(5X,4E15.6)
004250
004260
C
RETUR'1
END
SUBROUTINE SOLVE(A,B,NM,MB,MMAX,KK)
DIMENSION A(1),B(1)
004270
004280
004290
004300
004310
C
C   SOLUTION OF SYMMETRIC BANDED EQUATIONS IN SINGLE SUBSCRIPT ARITH. 004320
C
004330
MB1=MB-1
NNN=NM-1
004340
004350
IF(KK.EQ.2) GO TO 2000
004360
II=1
004370
DO 300 N=1,NNN
004380
CC=A(II)
004390
IF(CC.EQ.0.0) GO TO 250
004400
J1=II+1
004410
J2=II+MB1
004420
NE=NN-N
004430
IF(NE.LT.MB1) J2=II+NE
004440
M=II-1
004450
DO 200 J=J1,J2
004460
M=M+MMAX
004470
IF(A(J).EQ.0.0) GO TO 200
004480
C=A(J)/CC
004490
K=M
004500
DO 100 I=J,J2
004510
K=K+1
004520
100 A(K)=A(K)-C*A(I)
004530
A(J)=C
004540
200 CONTINUE
004550
250 CONTINUE
004560
II=II+MMAX
004570
300 CONTINUE
004580
RETUR'1
004590
2000 II=1
004600
DO 500 N=1,NNN
004610
CC=A(II)
004620
IF(CC.EQ.0.0) GO TO 450
004630
J1=II+1
004640
J2=II+MB1
004650
NE=NN-N
004660
IF(NE.LT.MB1) J2=II+NE
004670
C=B(N)
004671

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L=N
DO 400 J=J1,J2
L=L+1
400 B(L)=B(L)-A(J)*C
B(N)=C/CC
450 CONTINUE
II=II+1
500 CONTINUE
CC=A(II)
IF(CC.NE.0.0) B(NN)=B(NN)/CC
N=NN
II=MMAX*(NN-2)+1
DO 700 I=2,NN
M=N-1
IF(A(II).EQ.0.0) GO TO 650
J1=II+1
J2=II+MB1
NE=NN-M
IF(NE.LT.MB1) J2=II+NE
C=B(N)
L=N
DO 600 J=J1,J2
L=L+1
600 C=C-A(J)*B(L)
B(N)=C
650 CONTINUE
II=II-MMAX
700 CONTINUE
RETURN
END
SUBROUTINE MODIFY(N,Q,A,B,NN,MB,MMAX)
DIMENSION A(MMAX,NN),B('NN)
C
C MODIFICATION FOR PRESCRIBED ESSENTIAL BOUNDARY CONDITIONS.
C
DO 100 J=2,MB
L=N-J+1
IF(L.LE.0) GO TO 50
B(L)=B(L) - A(J,L)*Q
A(J,L)=0.0
50 L=N+J-1
IF(L.GT.NN) GO TO 100
B(L)=B(L) - A(J,N)*Q
100 A(J,N) = 0.0
B(N) = Q
A(1,N) = 0.0
RETURN
END
SUBROUTINE GRID(YCORD,NODE,NODES,NUMEL )
DIMENSION YCORD(30),NODE(2,30)
C THIS SUBROUTINE GENERATES NON-DIMENSIONAL CO-ORDINATES OF NODAL
C POINTS.
C     Y = BAR = Y / (HT/2) .
DY1 = 0.05
DY2 = 0.09375000
DY = DY2
YI = -1.0
DO 100 N = 1, NODES
YCORD(N) = YI
YI = YI + DY
DY = DY2
IF(N.GT.7.AND.N.LT.18) DY = DY1
100 CONTINUE

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005210
005221
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005223
005230
005240
005250
005260
005263
005264
005270
005280

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C      GENERATE NODE NUMBERS          005290
C
NO = 1
DO 200 N = 1,NUMEL
NODE(1,N) = NO
NODE(2,N) = NO + 1
NO = NO + 1
200 CONTINUE
RETURN
END
SUBROUTINE DISTURB(YCORD,NODE,EGDOT,DDDOT, ALFA,CN,
+ EPSILON,NUMEL,NINT,TEMP,TMP,NODES,HTMP )
COMMON/SHAPES/SHAPO(2,5),SHAP1(2,5),DSHAPO(2,5),DSHAP1(2,5),
+ DDSHAPO(2,5),DDSHAP1(2,5),SHAPB(2,5),DSHAPB(2,5)
DIMENSION YCORD(30),NODE(2,30),EGDOT(5,30),DDDOT(5,30)
+ ,TMP(31),TEMP(5,30)
WRITE(6,2010)
2010 FORMAT(9X,'NODAL VALUES OF VARIABLES CAUSED BY THE DISTURBANCE'/
+ 5X,'ELE. # INT. PT. #' ,9X,'GAMADOT',9X,'D-DOT',15X,'TEMP.')
DO 100 NEL = 1, NUMEL
I1= NODE(1,NEL)
I2 = NODE(2,NEL)
DO 100 INT = 1, NINT
S = SHAPB(1,INT)*YCORD(I1) + SHAPB(2,INT)*YCORD(I2)
FAC = (1.0-S*S)
FACN = FAC**CN
EXPV = EXP(-ALFA*S*S)
EGDOT(INT,NEL) = 0.0
DDDOT(INT,NEL) = 0.0
TEMP(INT,NEL) = HTMP + EPSILON*FACN*EXPV
WRITE(6,2000)NEL,INT,S,EGDOT(INT,NEL),DDDOT(INT,NEL),TEMP(INT,NEL)
2000 FORMAT(5X,2I5,4E15.5)
100 CONTINUE
DO 200 I=1,NODES
S = YCORD(I)
TMP(I) = HTMP + ((1.-S*S)**CN)*EPSILON*(EXP(-ALFA*S*S))
WRITE(6,2000) I,I,S,TMP(I)
200 CONTINUE
RETURN
END
SUBROUTINE THERM(TEMP, WORK, FAC1, NUMEL,NINT,NTT,DT,TMP
+,YCORD,NODES,NODE)
COMMON/SHAPES/SHAPO(2,5),SHAP1(2,5),DSHAPO(2,5),DSHAP1(2,5),
+ DDSHAPO(2,5),DDSHAP1(2,5),SHAPB(2,5),DSHAPB(2,5)
DIMENSION TEMP(5,30),WORK(5,30),NODE(2,30),YT(2),YCORD(30)
DIMENSION TMP(31),DISSIP(31),HEAT(2,31),
+ THCOND(31,31),FORCE(31)
DIMENSION LD(3),TH(6),EMASS(6),WEIGHT(4)
DATA WEIGHT/0.347854845137454, 0. 652145154862546,
+ 0.652145134862546,0.347854845137454/
C
C      GENERATE THE MATRICES          006120
C
MB = 2
DO 250 I = 1 , NODES
FORCE(I) = 0.0
IF(NTT.NE.1) GO TO 250
DO 230 J = 1, MB
230 HEAT(J,I) = 0.0
DO 231 J = 1,NODES
231 THCOND( J, I ) = 0.0
250 CONTINUE
DO 900 NEL = 1,NUMEL
DO 300 I = 1, 2

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II = NODE(I,NEL)          006290
YT(I) = YCORD(II)          006260
300 CONTINUE               006270
IF(NTT.NE.1) GO TO 510     006290
MC = 0                     006300
DO 400 I = 1, 2            006310
DO 400 J = 1, I            006320
MC = MC + 1                006330
TH(MC) = 0.0                006340
400 EMASS(MC) = 0.0         006350
MC = 0                     006360
DO 500 I = 1, 2            006370
DO 500 J = 1, I            006380
MC = IC + 1                006390
DJAC = (YT(2) - YT(1))*0.50 006400
IF(DJAC.LT.1.0E-10) GO TO 299 006410
DO 450 INT = 1,NINT        006415
WT = WEIGHT(INT)*DJAC      006420
WT1 = WEIGHT(INT)/DJAC      006430
EMASS(MC) = EMASS(MC) + SHAPB(I,INT)*SHAPB(J,INT)*WT 006440
TH(MC) = TH(MC) + DSHAPB(I,INT)*DSHAPB(J,INT)*WT1    006450
450 CONTINUE               006460
500 CONTINUE               006470
510 CONTINUE                006480
DO 550 I = 1, 2            006490
DISSIP(I) = 0.0              006500
DJAC = (YT(2) - YT(1))*0.50 006510
DO 550 INT = 1, NINT        006520
DJAC = DSHAPB(1,INT)*YT(1) + DSHAPB(2,INT)*YT(2) 006530
WT = WEIGHT(INT) * DJAC      006540
DISSIP(I) = DISSIP(I) + SHAPB(I,INT)*WORK(INT,NEL)*WT 006550
550 CONTINUE               006560
C ASSEMBLE THE GLOBAL MATRICES 006570
C                                     006580
DO 600 II = 1,2            006590
I=NODE(II,NEL)              006600
600 LD(II) = I                006610
MC = 0                     006620
DO 700 II = 1,2            006630
I=LD(II)                   006640
FORCE(I) = FORCE(I) + DISSIP(II) 006650
IF(NTT.NE.1) GO TO 700       006660
DO 690 JJ = 1, II            006670
MC = MC + 1                006680
M = LD(JJ)                  006690
IR = MINO(I,M)              006700
IC = IABS(I-M) + 1           006710
HEAT(IC,IR) = HEAT(IC,IR) + EMASS(MC) 006720
THCOND(I,M) = THCOND(I,M) + TH(MC)*FAC1 006730
THCOND(M,I) = THCOND(I,M) 006740
690 CONTINUE               006750
700 CONTINUE               006760
700 CONTINUE               006770
900 CONTINUE               006780
DO 950 I = 1,NODES          006790
IM1=I-1                    006792
IF(I.EQ.1) IM1 = 1           006793
IP1 = I+1                  006794
IF(I.EQ.NODES) IP1 = I      006795
DO 945 J = IM1,IP1          006800
945 FORCE(I) = FORCE(I) - THCOND(I,J)*TMP(J) 006810
950 CONTINUE               006812
IF(NTT.EQ.1)                 006840
+CALL SOLVE(HEAT, FORCE, NODES, M8, M8, 1) 006870
CALL SOLVE(HEAT, FORCE, NODES, M8, M8, 2) 006880

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      DO 991 N=1,NODES
      TMP(N) = TMP(N) + F1*DF(N)*DT
      990 CONTINUE
      C
      DO 995 NEL = 1,NUMEL
      I1 = NODE(1,NEL)
      I2 = NODE(2,NEL)
      DO 995 INT = 1,MINT
      995 TEMP(INT,NEL) = TMP(I1)*SHAPE(1,INT) + TMP(I2)*SHAPE(2,INT)
      RETURN
      997 WRITE(6,2400) NEL,NINT,DJAC
      2400 FORMAT(5X,'DJAC FOR ELE.',I5,'INT. PT.',I5,I5,E15.5//
      * 5X,'IT IS EXECUTION OF THE PROGRAM IS BEING STOPPED IN SUB. THERM')C07060
      STOP
      END
      SUBROUTINE DDOT(DDOT,INT,NEL,NODE,VELDOT,TGDOT,YCORD,EGDOT
      * , DT,NUZERO,NTT)
      COMMON/SHAPEC/SHAPO(2,5),SHAPE(2,5),DSHAPO(2,5),DSHAPI(2,5),
      * DDSHAPO(2,5),DOSHAPO(2,5),SHAPE(2,5),DSHAPB(2,5)
      DIMENSION DDOT(5,30),NODE(2,30),VELDOT(31),TGDOT(31),
      * YCORD(30),EGDOT(5,30)
      C
      C      THIS SUBROUTINE COMPUTES TOTAL D-DOT AND TOTAL G-DOT.
      C
      C      IF(INTT.LF.5) WRITE(5,2010)
      2010 FORMAT(5X,'ELE.# INT. PT. #      TOTAL G-DOT',5X,'TOTAL D-DOT')//I
      C
      DO 200 NEL = 1, NUMEL
      I1 = NODE(1,NEL)
      I2 = NODE(2,NEL)
      DJACI = 2.0/(YCORD(I2) - YCORD(I1))
      DO 200 INT = 1, MINT
      DDOT(INT,NEL) = DDOT(INT,NEL) + (DT*DJACI*DJACI)*
      * (DSHAPO(1,INT)*VELDOT(I1) + DSHAPB(1,INT)*VELDOT(I2) +
      * DDSHAPO(1,INT)*VELDOT(I1) + DOSHAPO(2,INT)*VELDOT(I2) +
      * DSHAPB(1,INT)*VELDOT(I1) + DSHAPB(2,INT)*VELDOT(I2) +
      * DSHAPI(1,INT)*TGDOT(I1) + DSHAPI(2,INT)*TGDOT(I2))
      EGDOT(INT,NEL) = EGDOT(INT,NEL) + DT*DJACI*
      * (DSHAPO(1,INT)*VELDOT(I1) + DSHAPB(2,INT)*VELDOT(I2) +
      * DSHAPB(1,INT)*TGDOT(I1) + DSHAPI(2,INT)*TGDOT(I2))
      C
      C      IF(INTT.LE.5)
      C      * WRITE(6,2000)NEL,INT,EGDOT(INT,NEL),DDOT(INT,NEL)
      2000 FORMAT(5X,2I5,2E15.5)
      200 CONTINUE
      RETURN
      END
      SUBROUTINE PLASTIC(EGDOT,DDOT,TGDOT,PDDOT,CM,GOOT,SIGMA,
      * CM,A,B,CMU,CW,DT,TAU0,TEMP,SIO,NTT,NUMEL,MINT,WORK,TAU
      * , HSI,HGP,HGPDT,PGAMA,SI,PSSTART,PD)
      DIMENSION EGDOT(5,30),DDOT(5,30),TGDOT(5,30),PDDOT(5,30)
      * ,PGAMA(5,100),SI(5,100),TEMP(5,30),TAU(5,30),SIGMA(5,30)
      * ,WORK(5,30),PD(5,100)
      C
      C      IF(IRESTART.EQ.0) GO TO 100
      C      IF(INTT.NE.1) GO TO 100
      C      INITIALIZE SI,PGDOT,PDDOT,TEMP,PGAMA,PD,SIGMA,TAU AT EACH POINT
      C
      DO 50 NEL = 1,NUMEL
      DO 50 INT = 1,MINT
      SI(INT,NEL)=HSI
      PGDOT(INT,NEL)=HGPDT
      PDDOT(INT,NEL)=0.0
      PGAMA(INT,NEL)=HGP
      PD(INT,NEL)=0.1
      TAU(INT,NEL)=TAU0
      SIGMA(INT,NEL)=0.0
      50
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      50 CONTINUE          0C7610
C     100 CONTINUE          007620
C
      DO 500 NEL = 1,NUMEL          007630
      DO 500 INT = 1,NINT          007640
      SII=SI(INT,NEL)          007650
      TMP=TEMP(INT,NEL)          007660
      CKAPAI = ((1.0+SI/SD0)**CHI)          007670
      CKAPA = CKAPAI * (1.0 - A*TMP)          007680
      ESTRES = SD0T ( TAU(INT,NEL)+TAU(INT,NEL) +
      + SIGMA(INT,NEL)-SIGMA(INT,NEL))          007700
      QT = ESTRES/CKAPA          007710
      IF(QT.LT.0.01) G7 TO 461          007720
      IF(QT.LT.1.0) G7 TO 450          007730
      R2 = QT**CHI - 1.0          0C7750
      GAMA = R2/(B*ESTRES+GD0T0)          0C7760
      SD0T = GAMA * ESTRES*ESTRES/CKAPA1          007770
      G0 T7 460          0C7780
C   450 CONTINUE          007785
      WRITE(6,2100) INT,NEL,ST          007790
      2100 FORMAT(5X,'THE INT. PT.',IS,' OF ELE. # ',I3,' IS UNLOADING.'/
      + 5X,'TAU/MAPA = ',E15.5)          0C7800
      GAYA = 0.0          007810
      SD0T = 1.0          007820
C   460 CONTINUE          007830
      GPDOT = GAMA * TAU(INT,NEL)          007840
      DPDOT = GAYA * STGMA(INT,NEL)          007850
      PGD0T(INT,NEL)=GPDOT          007860
      PDD0T(INT,NEL)=DPDOT          007870
      PDD0T(INT,NEL)=DPDT          007880
      SII(INT,NEL) = SI(INT,NEL) + SD0T*DT          007890
      PGAMA(INT,NEL) = PGAMA(INT,NEL) + GPDOT*DT          007900
      PD(INT,NEL) = PD(INT,NEL) + DPDOT*DT          007910
      C   WRITE(6,2000) NEL,INT,SD0T,GPDOT,DPDT          007920
      2000 F0RMAT(5X,2I9,3E15.5)          007930
      WORK(INT,NEL) = CKAPAI * SD0T
      TAU0T = CHI*(EGD0T(INT,NEL) - GPDOT)
      SIGDT = CHI*(DOD0T(INT,NEL) - DPDOT)
      TAU(INT,NEL) = TAU(INT,NEL) + TAU0T*DT
      SIGMA(INT,NEL) = SIGMA(INT,NEL) + SIGDT*DT
C   500 CONTINUE          007940
      G7 T7 462          007950
      461 WRITE(6,2010) QT          007960
      2010 FORMAT(///5X,'THE EXECUTION OF THE PROGRAM IS BEING
      + STOPPED. QT = ',E15.5)          007970
      STOP          007980
C   462 CONTINUE          007990
      RETURN          008000
      END          008010

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